

Bubble and Selection Sorts

Objectives

- ◆ In this Week, you will learn to:
 - ◆ Identify the algorithms that can be used to sort data
 - ◆ Sort data by using bubble sort
 - ◆ Sort data by using selection sort

Sorting Data

- ◆ Sorting is the process of arranging data in some pre-defined order or sequence. The order can be either ascending or descending.
- ◆ If the data is ordered, you can directly go to the section , thereby reducing the number of records to be traversed.

Selecting a Sorting Algorithm

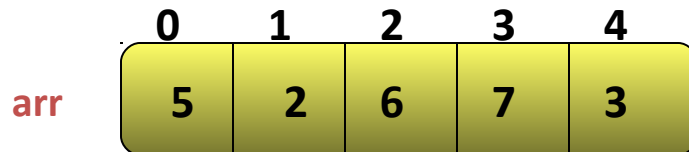
- ◆ Sorting is implemented in a program by using an algorithm.
- ◆ Some sorting algorithms are:
 - ◆ Bubble sort
 - ◆ Selection sort
 - ◆ Insertion sort
 - ◆ Shell sort
 - ◆ Merge sort
 - ◆ Quick sort

Sorting data by Using Bubble Sort

- ◆ Bubble sort algorithm:
 - ◆ Is one of the simplest sorting algorithms
 - ◆ Has a quadratic order of growth and is therefore suitable for sorting small lists only
 - ◆ Works by repeatedly scanning through the list, comparing adjacent elements, and swapping them if they are in the wrong order

Implementing Bubble Sort Algorithm

- ◆ To understand the implementation of bubble sort algorithm, consider an unsorted list of numbers stored in an array.



Implementing Bubble Sort Algorithm (Contd.)

◆ Let us sort this unsorted list.

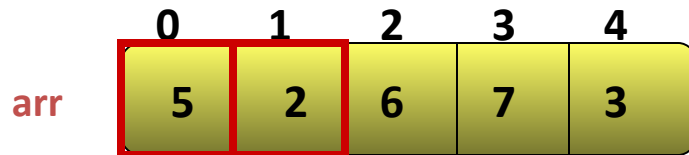
	0	1	2	3	4
arr	5	2	6	7	3

Implementing Bubble Sort Algorithm (Contd.)

Pass 1

$n = 5$

- ◆ Compare the element stored at index 0 with the element stored at index 1.

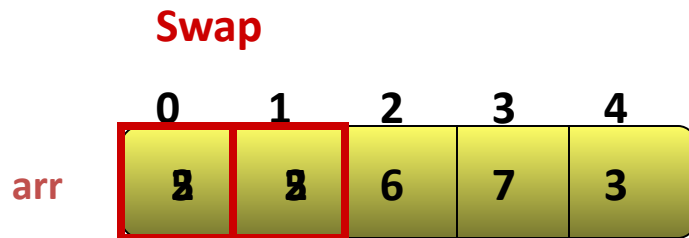


Implementing Bubble Sort Algorithm (Contd.)

Pass 1

n = 5

◆ Swap the values if they are not in the correct order.



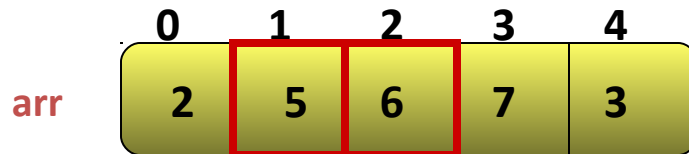
Implementing Bubble Sort Algorithm (Contd.)

Pass 1

n = 5

- ◆ Compare the element stored at index 1 with the element stored at index 2 and swap the values if the value at index 1 is greater than the value at index 2.

No Change

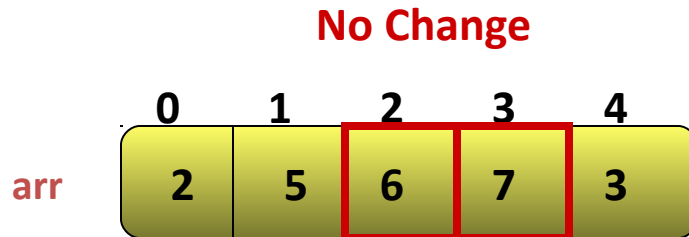


Implementing Bubble Sort Algorithm (Contd.)

Pass 1

$n = 5$

- ◆ Compare the element stored at index 2 with the element stored at index 3 and swap the values if the value at index 2 is greater than the value at index 3.

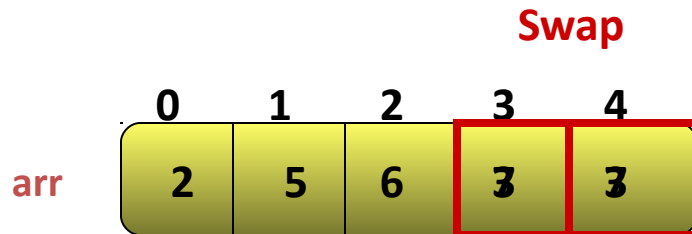


Implementing Bubble Sort Algorithm (Contd.)

Pass 1

$n = 5$

- ◆ Compare the element stored at index 3 with the element stored at index 4 and swap the values if the value at index 3 is greater than the value at index 4.

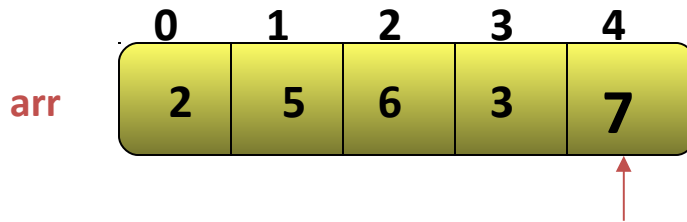


Implementing Bubble Sort Algorithm (Contd.)

Pass 1

$n = 5$

- ◆ Compare the element stored at index 3 with the element stored at index 4 and swap the values if the value at index 3 is greater than the value at index 4.



Largest element is placed at its correct position after Pass 1

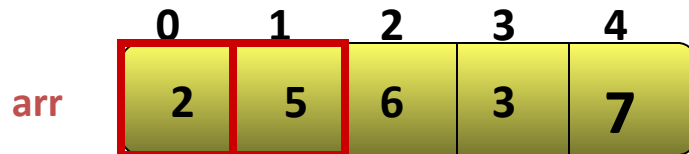
Implementing Bubble Sort Algorithm (Contd.)

Pass 2

n = 5

- ◆ Compare the element stored at index 0 with the element stored at index 1 and swap the values if the value at index 0 is greater than the value at index 1.

No Change



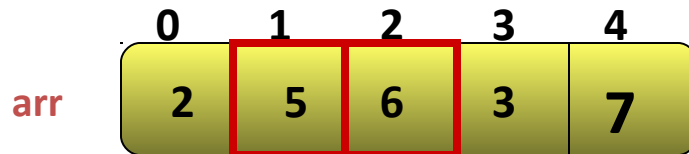
Implementing Bubble Sort Algorithm (Contd.)

Pass 2

$n = 5$

- ◆ Compare the element stored at index 1 with the element stored at index 2 and swap the values if the value at index 1 is greater than the value at index 2.

No Change

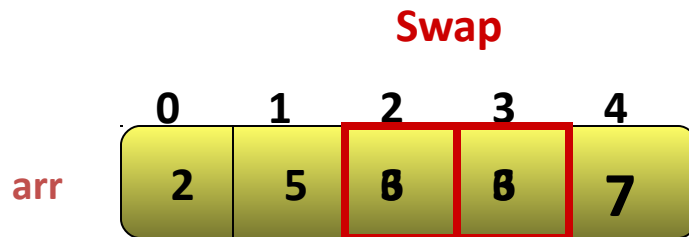


Implementing Bubble Sort Algorithm (Contd.)

Pass 2

$n = 5$

- ◆ Compare the element stored at index 2 with the element stored at index 3 and swap the values if the value at index 2 is greater than the value at index 3.

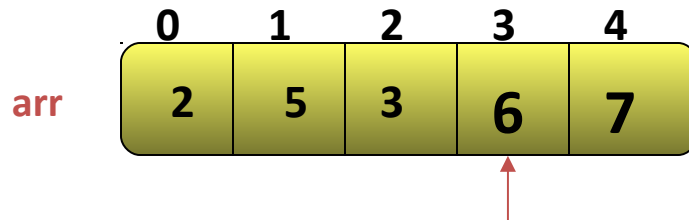


Implementing Bubble Sort Algorithm (Contd.)

Pass 2

$n = 5$

- ◆ Compare the element stored at index 2 with the element stored at index 3 and swap the values if the value at index 2 is greater than the value at index 3.



Second largest element is placed at its correct position after Pass 2

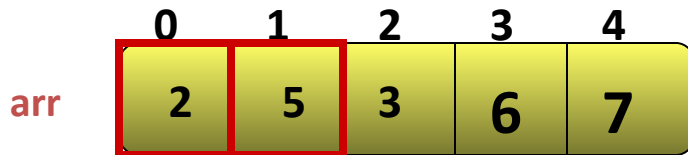
Implementing Bubble Sort Algorithm (Contd.)

Pass 3

n = 5

- ◆ Compare the element stored at index 0 with the element stored at index 1 and swap the values if the value at index 0 is greater than the value at index 1.

No Change

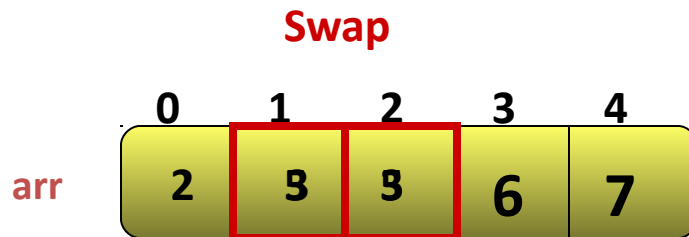


Implementing Bubble Sort Algorithm (Contd.)

Pass 3

n = 5

- ◆ Compare the element stored at index 1 with the element stored at index 2 and swap the values if the value at index 1 is greater than the value at index 2.

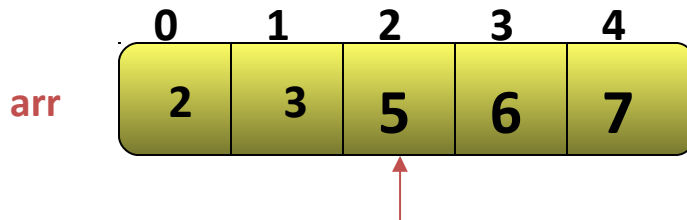


Implementing Bubble Sort Algorithm (Contd.)

Pass 3

$n = 5$

- ◆ Compare the element stored at index 2 with the element stored at index 3 and swap the values if the value at index 2 is greater than the value at index 3.



Third largest element is placed at its correct position after Pass 3

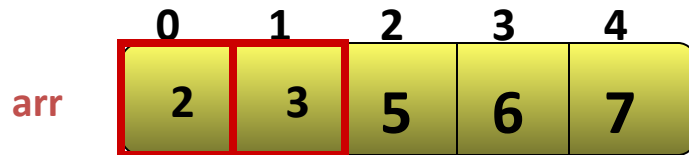
Implementing Bubble Sort Algorithm (Contd.)

Pass 4

n = 5

- ◆ Compare the element stored at index 0 with the element stored at index 1 and swap the values if the value at index 0 is greater than the value at index 1.

No Change

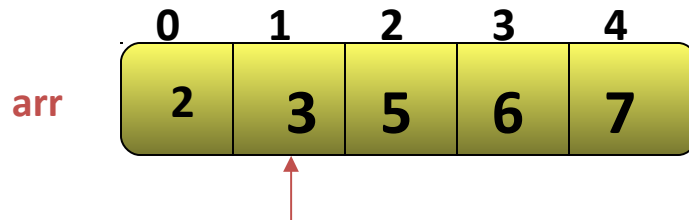


Implementing Bubble Sort Algorithm (Contd.)

Pass 4

$n = 5$

- ◆ Compare the element stored at index 0 with the element stored at index 1 and swap the values if the value at index 0 is greater than the value at index 1.



Fourth largest element is placed at its correct position after Pass 4

Implementing Bubble Sort Algorithm (Contd.)

Pass 4

$n = 5$

◆ At the end of Pass 4, the elements are sorted.

	0	1	2	3	4
arr	2	3	5	6	7

Implementing Bubble Sort Algorithm (Contd.)

Algorithm BubbleSort (A [],n)

{

1. for (pass = 1 to n-1)

 1.1 for (j= 0 to n – 1 – pass)

 1.1.1 If (A [j] > A [j+1])

 1.1.1.1 t = A [j]

 1.1.1.2 A [j] = A [j+1]

 1.1.1.3 A [j+1] = t

}

Determining the Efficiency of Bubble Sort Algorithm

- ◆ The efficiency of a sorting algorithm is measured in terms of number of comparisons.
- ◆ In bubble sort, there are $n - 1$ comparisons in Pass 1, $n - 2$ comparisons in Pass 2, and so on.
- ◆ Total number of comparisons = $(n - 1) + (n - 2) + (n - 3) + \dots + 3 + 2 + 1 = n(n - 1)/2$.
- ◆ $n(n - 1)/2$ is of $O(n^2)$ order. Therefore, the bubble sort algorithm is of the order $O(n^2)$.

Just a minute

◆ What is the order of growth of the bubble sort algorithm?

◆ Answer:

◆ The bubble sort algorithm has a quadratic order of growth.

Just a minute

◆ While implementing bubble sort algorithm, how many comparisons will be performed in Pass 1.

◆ Answer:

◆ $n - 1$ comparisons

Sorting Data by Using Selection Sort

- ◆ Selection sort algorithm:
 - ◆ Has a quadratic order of growth and is therefore suitable for sorting small lists only
 - ◆ Scans through the list iteratively, selects one item in each scan, and moves the item to its correct position in the list

Implementing Selection Sort Algorithm

- ◆ To understand the implementation of selection sort algorithm, consider an unsorted list of numbers stored in an array.

	0	1	2	3	4
arr	105	120	10	200	20

Implementing Selection Sort Algorithm (Contd.)

◆ Let us sort this unsorted list.

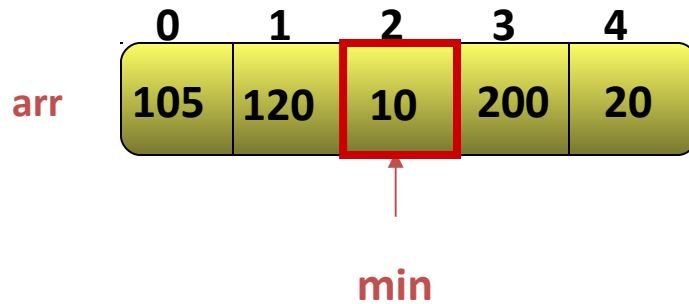
	0	1	2	3	4
arr	105	120	10	200	20

Implementing Selection Sort Algorithm (Contd.)

Pass 1

$n = 5$

- ◆ Search the minimum value in the array, $arr[0]$ to $arr[n - 1]$.

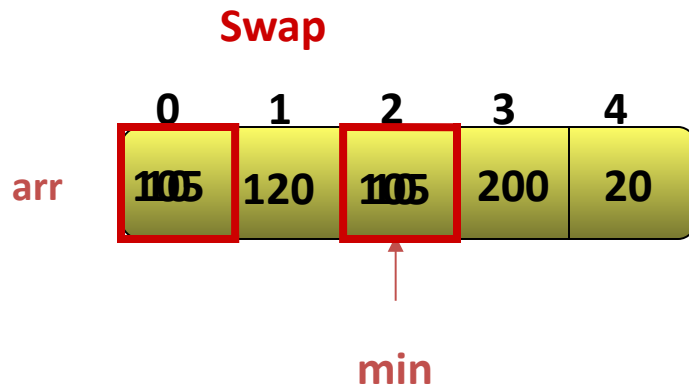


Implementing Selection Sort Algorithm (Contd.)

Pass 1

$n = 5$

- ◆ Search the minimum value in the array, $arr[0]$ to $arr[n - 1]$.
- ◆ Swap the minimum value with the value at index 0.

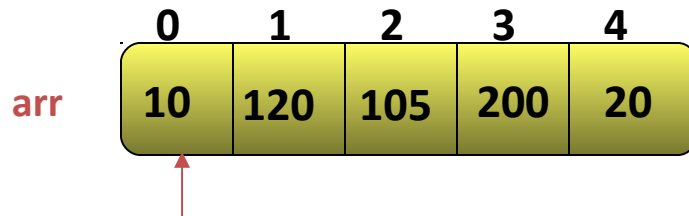


Implementing Selection Sort Algorithm (Contd.)

Pass 1

$n = 5$

- ◆ Search the minimum value in the array, $arr[0]$ to $arr[n - 1]$.
- ◆ Swap the minimum value with the value at index 0.



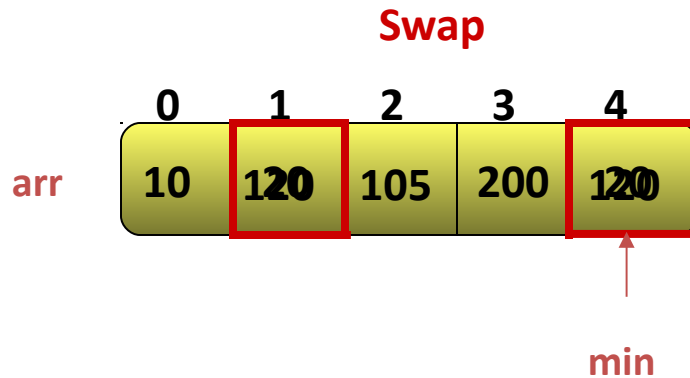
The smallest value is placed at its correct location after Pass 1

Implementing Selection Sort Algorithm (Contd.)

Pass 2

$n = 5$

- ◆ Search the minimum value in the array, $arr[1]$ to $arr[n - 1]$.
- ◆ Swap the minimum value with the value at index 1.

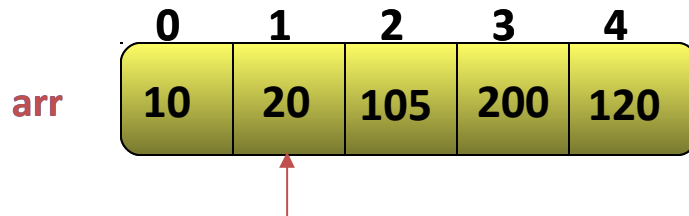


Implementing Selection Sort Algorithm (Contd.)

Pass 2

$n = 5$

- ◆ Search the minimum value in the array, $arr[1]$ to $arr[n - 1]$.
- ◆ Swap the minimum value with the value at index 1.



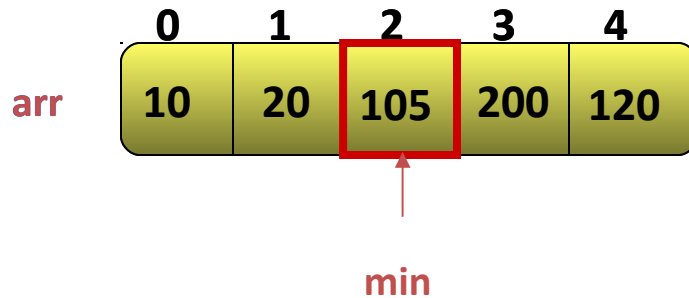
The second smallest value is placed at its correct location after Pass 2

Implementing Selection Sort Algorithm (Contd.)

Pass 3

$n = 5$

- ◆ Search the minimum value in the array, $\text{arr}[2]$ to $\text{arr}[n - 1]$.
- ◆ Swap the minimum value with the value at index 2.

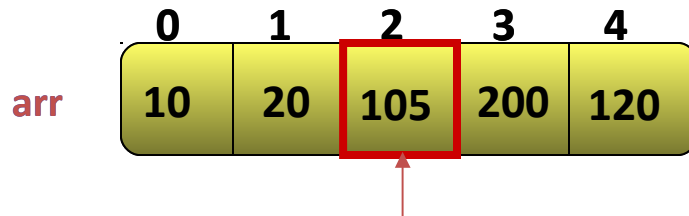


Implementing Selection Sort Algorithm (Contd.)

Pass 3

$n = 5$

- ◆ Search the minimum value in the array, $arr[2]$ to $arr[n - 1]$.
- ◆ Swap the minimum value with the value at index 2.



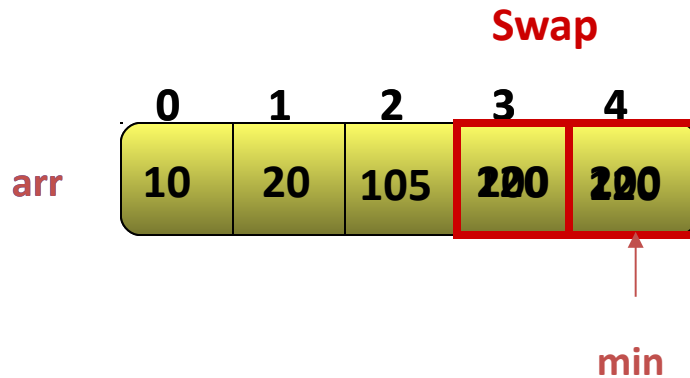
The third smallest value is placed at its correct location after Pass 3

Implementing Selection Sort Algorithm (Contd.)

Pass 4

$n = 5$

- ◆ Search the minimum value in the array, $arr[3]$ to $arr[n - 1]$.
- ◆ Swap the minimum value with the value at index 3.

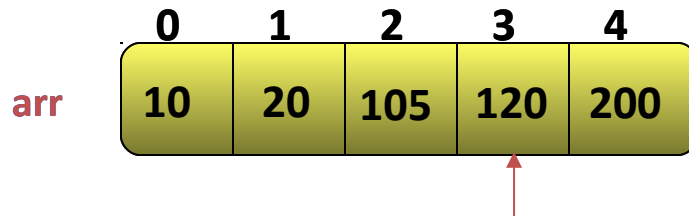


Implementing Selection Sort Algorithm (Contd.)

Pass 4

$n = 5$

- ◆ Search the minimum value in the array, $\text{arr}[3]$ to $\text{arr}[n - 1]$.
- ◆ Swap the minimum value with the value at index 3.



The fourth smallest value is placed at its correct location after Pass 4

Implementing Selection Sort Algorithm (Contd.)

Pass 4

$n = 5$

◆ The list is now sorted.

	0	1	2	3	4
arr	10	20	105	120	200

Implementing Selection Sort Algorithm (Contd.)

Algorithm SelectionSort (A [],n)

{

1. for(i = 0 to n-2)

 1.1 Set min = i

 1.2 for (j= i+1 to n-1)

 1.2.1 if (A [j] < A [min])

 1.2.1.1 min = j

 1.3 swap A [i] and A [min]

}

Determining the Efficiency of Selection Sort Algorithm

- ◆ In selection sort, there are $n - 1$ comparisons during Pass 1 to find the smallest element, $n - 2$ comparisons during Pass 2 to find the second smallest element, and so on.
- ◆ Total number of comparisons = $(n - 1) + (n - 2) + (n - 3) + \dots + 3 + 2 + 1 = n(n - 1)/2$
- ◆ $n(n - 1)/2$ is of $O(n^2)$ order. Therefore, the selection sort algorithm is of the order $O(n^2)$.

Just a minute

- ◆ Read the following statement and specify whether it is true or false:
 - ◆ The efficiency of selection sort algorithm is same as that of the bubble sort algorithm.

- ◆ Answer:
 - ◆ True

Just a minute

◆ How many comparisons are performed in the second pass of the selection sort algorithm?

◆ Answer:

◆ $n - 2$